

1 **Modeling Spatial and Temporal Variability of Residential Air Exchange Rates for**
2 **the Near-Road Exposures and Effects of Urban Air Pollutants Study (NEXUS)**

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Abstract

25 Air pollution health studies often use outdoor concentrations as exposure surrogates. Failure to
26 account for variability of residential infiltration of outdoor pollutants can lead to exposure
27 misclassifications and add error to risk estimates. The residential air exchange rate (AER), which
28 is the rate of exchange of indoor air with outdoor air, is an important determinant for house-to-
29 house (spatial) and temporal variations of air pollution infiltration. Our goal was to perform a
30 cross validation, and then apply mechanistic models to predict AERs for 213 homes in the Near-
31 Road Exposures and Effects of Urban Air Pollutants Study (NEXUS), a cohort study of traffic-
32 related air pollution exposures and respiratory effects in asthmatic children living near major
33 roads in Detroit, Michigan. We used a previously developed model (LBL), which predicts AER
34 from meteorology and questionnaire data on building characteristics related to air leakage, and
35 an extended version of this model (LBLX) that includes natural ventilation from open windows.
36 As a critical and novel aspect of our AER modeling approach, we performed a cross validation,
37 which included both parameter estimation (i.e., model calibration) and model evaluation, based
38 on daily AER measurements from a subset of 24 study homes on five consecutive days during
39 two seasons. The measured AER varied between 0.09 and 3.48 h^{-1} with a median of 0.64 h^{-1} . For
40 the individual model-predicted and measured AER, the median absolute difference was 29%
41 (0.19 h^{-1}) for both the LBL and LBLX models. The LBL and LBLX models predicted 59% and
42 61% of the variance in the AER, respectively. Daily AER predictions for all 213 homes during
43 the three year study (2010 – 2012) showed considerable house-to-house variations from building
44 leakage differences, and temporal variations from outdoor temperature and wind speed
45 fluctuations. Using this novel approach, NEXUS will be one of the first epidemiology studies to
46 apply calibrated and home-specific AER models, and to include the spatial and temporal

47 variations of AER for over 200 individual homes across multiple years into an exposure

48 assessment in support of improving risk estimates.

49

50

Introduction

51 Numerous air pollution epidemiology studies have found associations between ambient
52 concentrations and adverse health effects.^{1,2} These health studies often estimate exposures using
53 data provided by ambient air monitors, which can lead to exposure misclassification due to time
54 spent in indoor microenvironments with pollutant concentrations that can be substantially
55 different from local ambient concentrations. This exposure misclassification can lead to error and
56 bias in health effect estimates.^{2,3} To reduce exposure misclassification, we are developing an air
57 pollution exposure model for individuals (EMI) in health studies.⁴⁻⁷ The EMI predicts personal
58 exposures based on outdoor concentrations, meteorology, questionnaire information (e.g.,
59 building characteristics, occupant behavior related to building operation), and time-location
60 information. A critical aspect of EMI is the air exchange rate (AER) of individual homes, which
61 is the rate of exchange of indoor air with outdoor air. In addition, AERs have been applied as a
62 covariate or modifying factor in air pollution epidemiology studies, showing the importance of
63 this variable.^{8,9}

64 This study addresses the cross-validation and application of residential AER models, and
65 specifically the AER predictions for the Near-Road Exposures and Effects of Urban Air
66 Pollutants Study (NEXUS).⁴ The goal of NEXUS is to examine traffic-related air pollution
67 exposures and respiratory effects in asthmatic children living near major roads in Detroit,
68 Michigan (MI).

69 The AER affects both the steady-state (i.e., long-term average) and dynamic (i.e., time-
70 varying) behaviors of indoor air pollutant concentrations, and the resulting exposures.¹⁰ For
71 example, assume that outdoor concentrations, C_{out_ss} are under steady-state conditions (i.e., short-

72 term changes of concentrations are considered negligible compared with long-term average
73 concentrations), then the steady-state indoor concentrations C_{in_ss} can be described by

74
$$C_{in_ss} = F_{inf} C_{out_ss} \quad (1)$$

75 where F_{inf} is the fraction of C_{out_ss} that enters and remains airborne indoors (infiltration factor)
76 defined as

77
$$F_{inf} = P \text{ AER}/(\text{AER}+k_d) \quad (2)$$

78 where P is the penetration coefficient, and k_d is the indoor loss rate. Setting $P=0.9$ and $k_d=1.0 \text{ h}^{-1}$
79 based on reported values for particulate matter (diameter = 2.5 μm ; PM_{2.5}), C_{in_ss} for a tight
80 (AER=0.1 h^{-1}) and leaky (AER=3.0 h^{-1}) building is 0.08 and 0.68 times C_{out_ss} , respectively.
81 Therefore, the AER can substantially affect C_{in_ss} . Furthermore, studies examining particulate
82 matter show that the AER can explain a substantial amount of the variability of F_{inf} .¹¹⁻¹³ For
83 time-varying outdoor concentrations C_{out} (e.g., traffic), indoor concentrations C_{in} can be
84 described by the dynamic mass balance equation

85
$$\frac{dC_{in}}{dt} = P \text{ AER } C_{out} - (\text{AER} + k_d)C_{in} \quad (3)$$

86 Measurements of C_{out} and C_{in} for time-varying traffic pollutants show that the dynamic behavior
87 of C_{in} depends on the AER;¹⁴ for example, C_{in} increases more slowly and reaches lower peak
88 levels for tighter buildings.¹⁵

89 For gaseous pollutants with $k_d > 0$ (e.g., ozone), F_{inf} depends on AER.¹⁶ For gases with
90 negligible k_d (e.g., carbon monoxide) compared with AER, C_{in_ss} can be considered independent
91 of the AER based on Equation 2 ($F_{inf}=P$).¹⁷ However, for outdoor pollutants that vary with time
92 (e.g., traffic), time-varying C_{in} (Equation 3) depends on AER even when k_d is negligible
93 compared with AER.¹⁴

94 A residential AER model has several benefits for exposure assessments in health studies.
95 First, the AER is a key determinant for the entry of outdoor-generated air pollutants and the
96 removal of indoor-generated air pollutants.^{10,18} Since people in the United States spend
97 approximately 66% of their time indoors at home,^{19,20} the residential AER is a critical parameter
98 for air pollution exposure models. Costs and participant burden often limit the number of AER
99 measurements. Therefore, a residential AER model integrated within exposure models can be a
100 feasible method to predict exposure metrics for epidemiological analysis. Second, an AER model
101 can reduce the uncertainty of exposure models by accounting for factors that influence the house-
102 to-house (spatial) and temporal variability of the AER. These factors include the physical driving
103 forces of the airflows (e.g., indoor-outdoor temperature differences, wind speed), building
104 characteristics (e.g., local wind sheltering, building height, tightness of the building envelope),
105 and occupant behavior (e.g., opening windows). Spatial and temporal differences in weather,
106 building characteristics, and occupant behavior can produce substantial AER variations. The
107 resulting spatial and temporal variations in exposure may help explain the impact of AER for
108 individuals with exceptionally high and low exposures. Also, predicting the AER variability can
109 help reduce exposure misclassifications, and the resulting errors in health effect estimates.

110 Various AER models are described in the literature.¹⁰ The Lawrence Berkeley Laboratory
111 (LBL) model is widely used to predict residential AER.²¹ The LBL model predicts the AER due
112 to airflow through small unintentional openings (i.e., leakage), but does not account for the
113 airflow through large controllable openings (i.e., natural ventilation), such as open windows.
114 Previously, we addressed this limitation by extending the LBL model (LBLX) to predict natural
115 ventilation airflow.⁶ In this study, we used the previously developed LBL and LBLX models,
116 which were linked with a leakage area model, to predict the AER from questionnaire and

117 weather data.⁶ The LBL model was used for all homes, and the LBLX model was used for a
118 subset of homes with window opening data, as described below.

119 The NEXUS design includes the development of various tiers of modeled exposure
120 metrics for traffic-related air pollutants, and the use of measurements from a subset of homes for
121 model calibration (i.e., parameter estimation) and evaluation.⁴ This paper focuses on modeling
122 the residential AER. We used NEXUS questionnaires and airport weather data as inputs for the
123 AER models, and AER measurements from a subset of homes for parameter estimation and
124 model evaluation. Below, we first describe the NEXUS design, and then describe the AER
125 models, methods for parameter estimation and model evaluation, and development of daily AER
126 predictions for the three year health study.

127

128 **Methods**

129 **NEXUS Design**

130 NEXUS was designed to examine the relationship between exposures to traffic-related air
131 pollutants and respiratory outcomes in a cohort of children with asthma living near major roads
132 in Detroit, MI.⁴ For this community-based participatory research study, children from 6 to 14
133 years of age with asthma or symptoms of asthma were recruited based on the proximity of their
134 home to major roads according to three traffic categories: (1) high diesel/high traffic (HTHD),
135 (2) high traffic/low diesel (HTLD), and (3) low traffic/low diesel (LTLD).⁴ A total of 147
136 children participated in the study from September 2010 to December 2012. Since children moved
137 during the study, a total of 213 residences were considered, which included 203 detached homes,
138 nine apartments, and one townhome. The study population consisted of 98 homes in the high
139 traffic categories (52 in HTHD, 46 in HTLD) and 115 homes in the low traffic category (LTLD).

140 An overview of the exposure assessment method in NEXUS has been previously
141 described.⁴ Residential indoor, residential outdoor, school outdoor, and near-highway air
142 monitoring was performed during two seasonal intensive field sampling periods: September 25
143 to November 11, 2010 (Fall 2010) and March 28 to May 4, 2011 (Spring 2011). The fall and
144 spring are peak seasons for respiratory viruses that can induce asthma symptoms. A subset of 24
145 homes was selected for residential monitoring during the seasonal intensives based on the traffic
146 characteristics of nearby roads, and consisted of 12 homes in the high traffic categories (7 in
147 HTHD, 5 in HTLD) and 12 homes in the low traffic category (LTLD). A maximum of four
148 residences were monitored simultaneously during a 5 day period.

149 Daily 24 h average AERs were measured for 5 consecutive days during the season
150 intensives in the 24 homes using a perfluorocarbon tracer (PFT) method.^{22,23} The Brookhaven
151 National Laboratory (BNL; Upton, NY) prepared the tracer sources and receptor tubes, and
152 provided guidance on the number of tracers sources required in each home. Sources were placed
153 in the homes 24 h before the first day of measurement to allow for sufficient distribution. The
154 reported accuracy (based on known AER), precision (based on replicate measurements), and
155 limits on the PFT-derived AER measurements for occupied homes are estimated to be 20-25%,
156 5-15%, and 0.2-5.0 h⁻¹, respectively.^{18,24,25}

157 These AER measurements were used for parameter estimation and evaluation of the AER
158 model, as described below. Input data for the AER models were obtained for meteorology,
159 housing characteristics, household income, and occupant behavior. Meteorological
160 measurements included local airport temperature and wind speed. During the seasonal intensives
161 on days with residential measurements, indoor temperatures were measured and occupants

162 recorded when certain activities related to housing operation were performed, including opening
163 windows.

164

165 **AER Model Overview**

166 The exchange of outdoor air with air inside occupied spaces of buildings can be separated into
167 three categories: leakage, natural ventilation, and mechanical ventilation.¹⁸ Leakage is the
168 airflow through unintentional opening in the building envelope (e.g., small cracks around
169 windows, exterior doors, joints between exterior walls and floors). Natural ventilation is the
170 intentional airflow through controlled openings in the building envelope (e.g., open windows and
171 doors). Mechanical ventilation is the airflow induced by outdoor-vented fans. For this study, we
172 used two AER models, one model that includes leakage (LBL) and another model that includes
173 both leakage and natural ventilation (LBLX).^{6,10} Mechanical ventilation was not considered
174 since detailed information on the specific type and operation of outdoor-vented fans was
175 unavailable from NEXUS.

176 The driving mechanism for airflows are pressure differences across the building
177 envelope.^{10,18} The pressure differences for leakage and natural ventilation are driven by indoor-
178 outdoor temperature differences (stack effect) and wind (wind effect). For this study, the LBL
179 and LBLX models include the stack and wind effects based on local airport temperature and
180 wind speed, and building characteristics (e.g., building height and wind sheltering from nearby
181 structures) that modify the stack and wind effect-driving forces.

182 Mechanistic AER models, which account for the physical driving forces of the airflows
183 (i.e., stack and wind effect) can be classified as single-zone and multizone models.¹⁰ Single-zone
184 models predict the AER for a whole building represented as a single, well-mixed compartment.

185 Multizone models are required for buildings that need to be represented by a series of
186 interconnected compartments with distinct pressures and temperatures. The LBL and LBLX
187 models are single-zone models that are appropriate for buildings with no internal resistance to
188 airflow, such as the homes included in this study.

189 We developed a computer simulation for the LBL and LBLX models linked to a leakage
190 area model. First, parameters for the leakage area model were estimated using the LBLX model
191 and the AER measurements and window opening data from a subset of homes. Then, daily (24 h
192 average) AER predictions were developed for every home for the three year health study. Since
193 window opening data was not available for the three year study, we used the LBL model to
194 develop AER predictions for the health study. Below, we first describe the AER models, and the
195 method for parameter estimation and model evaluation. The complete method and subsequent
196 analysis were implemented using MATLAB software (version R2014a, Mathworks, Natick,
197 MA).

198

199 ***LBL Leakage Model***

200 The LBL and LBLX models were previously described and evaluated for homes in central North
201 Carolina.⁶ Briefly, the LBL model predicts the AER due to leakage, and assumes the building is
202 a single, well-mixed compartment. The leakage airflow Q_{LBL} is calculated as

$$203 Q_{LBL} = A_{leak}\sqrt{k_s|T_{in} - T_{out}| + k_w U^2} \quad (4)$$

204 where A_{leak} is the effective air leakage area, k_s is the stack coefficient, k_w is the wind coefficient,
205 T_{in} and T_{out} are the average indoor and outdoor temperatures over time interval of calculation,
206 respectively, and U is the average wind speed over time interval of calculation. The stack and

207 wind effects are the first and second terms within the square root in Equation 4, respectively. The
208 AER is calculated as Q_{LBL} divided by the building volume V .

209 The AER has two parameters (k_s and k_w) and five inputs (A_{leak} , T_{in} , T_{out} , U , and V).
210 Parameters k_s and k_w were set to literature-reported values based on house-specific information
211 on house height (number of stories) and local wind sheltering (Supplementary Material Table
212 S1-S3). The number of stories and local wind sheltering were determined from aerial and
213 street-level images in Google Earth (version 7.1.2.2041; Google, Mountain View, CA, USA).
214 We used house numbers visible in street-level images to verify the study participant homes. To
215 determine V , we multiplied the floor area A_{floor} by the measured ceiling height (typically 2.44 m,
216 8 ft). The A_{floor} were both measured and obtained from online city and real estate databases of
217 property records (BS&A Software, Bath, MI, USA; Zillow, Seattle WA, USA; Trulia, San
218 Francisco, CA, USA).

219 We determined T_{out} and U (10 m elevation) from hourly measurements at the Detroit
220 Metro Airport in Detroit, MI. For parameter estimation, we calculated the 24 h average T_{out} and
221 U time-matched to the 24 h average AER measurements. To develop AER predictions for all
222 homes across the three year study period, we used hourly T_{out} and U to predict hourly AER, and
223 then calculated daily (24 h average) AER.

224 We determined T_{in} from continuous (5 min) indoor measurements. For parameter
225 estimation, we calculated the 24 h average T_{in} time-matched to the 24 h average AER
226 measurements. For developing AER predictions for all homes across the three year study period,
227 we set T_{in} to the 24 °C, which is the overall median of 1 h average T_{in} from a subset of 59 homes
228 across 6 seasons. We used a constant value for T_{in} since the seasonal medians of the T_{in} did not

229 vary substantially (24, 24, 24, 25, 23, 23 °C in fall 2010, winter 2010, spring 2011, summer
230 2011, fall 2011, winter 2011; respectively).

231 We estimated A_{leak} with a literature-reported leakage area model.^{6,26} The A_{leak} is
232 calculated as

$$233 \quad A_{\text{leak}} = NL/NF \quad (5)$$

234 where NL is the normalized leakage and NF is the normalization factor. NL was estimated from
235 the year built Y_{built} and A_{floor} as described by

$$236 \quad NL = \exp(\beta_0 + \beta_1 Y_{\text{built}} + \beta_2 A_{\text{floor}}) \quad (6)$$

237 where β_0 , β_1 , and β_2 are the regression parameters. The NF is defined as

$$238 \quad NF = (1000/A_{\text{floor}})(H/2.5)^{0.3} \quad (7)$$

239 where H is the building height. We set H to the number of stories multiplied by a story height of
240 2.5 m and adding a roof height of 0.5 m.⁶ The A_{floor} was obtained as described above and Y_{built}
241 was obtained from online city and real estate databases of property records (BS&A Software,
242 Bath, MI, USA; Zillow, Seattle WA, USA; Trulia, San Francisco, CA, USA).

243

244 ***LBLX Leakage + Natural Ventilation Model***

245 The LBLX model predicts the AER due to leakage and natural ventilation. The airflow is
246 calculated as

$$247 \quad Q_{\text{LBLX}} = \sqrt{Q_{\text{LBL}}^2 + Q_{\text{nat}}^2} \quad (8)$$

248 Where Q_{LBL} is the leakage airflow as defined above, and Q_{nat} is the natural ventilation airflow
249 through open windows.⁶ The AER is calculated as Q_{LBLX} divided by V.

250 The airflow for natural ventilation Q_{nat} is calculated as

$$251 \quad Q_{\text{nat}} = \sqrt{Q_{\text{nat_wind}}^2 + Q_{\text{nat_stack}}^2} \quad (9)$$

252 where $Q_{\text{nat,wind}}$ and $Q_{\text{nat,stack}}$ are the airflows from the wind and stack effects, respectively. The
253 $Q_{\text{nat,wind}}$ is defined as

254
$$Q_{\text{nat,wind}} = C_v A_{\text{nat}} U \quad (10)$$

255 where C_v is the effectiveness of the openings, and A_{nat} is the area of the inlet openings. Using the
256 literature-reported method, we set C_v to 0.30 and A_{nat} to one-half of the total area of window
257 openings.⁶ We calculated the 24 h average total area of window openings from daily window
258 opening data (number of windows opened multiplied by fraction of day) multiplied by window
259 opening area of 0.06 m² (derived from literature-reported window width of 0.6 m and height of
260 0.1 m).⁶ The $Q_{\text{nat,stack}}$ is defined as

261
$$Q_{\text{nat,stack}} = \frac{C_D A_{\text{nat}} \sqrt{2g \Delta H_{\text{NPL}} |T_{\text{in}} - T_{\text{out}}|}}{\max\{T_{\text{in}}, T_{\text{out}}\}} \quad (11)$$

262 where C_D is the discharge coefficient for the openings, g is the gravitational acceleration, ΔH_{NPL}
263 is the height from midpoint of lower window opening to the neutral pressure level (NPL) of the
264 building, and $\max\{T_{\text{in}}, T_{\text{out}}\}$ is the maximum value between T_{in} and T_{out} . Using literature-reported
265 values, we set C_D to 0.65, the midpoint of lower window opening to 0.91 m, and the NPL to one-
266 half of the building height.⁶ The building height is set to the number of stories multiplied by a
267 story height of 2.5 m and adding a roof height of 0.5 m.

268

269 ***Parameters for A_{leak} and Cross Validation***

270 We estimated the parameters (β_0 , β_1 , and β_2) for A_{leak} (Equation 6) using the AER measurements.
271 The subset of homes with measured AERs consisted of a cluster of 23 older homes built between
272 1900 and 1969 (median 1942), and one newer home built in 1997 (Supplementary Material
273 Figure S1). Since the cluster of 23 homes were substantially older than the home built in 1997,
274 we used the cluster of 23 homes for parameter estimation. We then applied the estimated

275 parameters for all homes built in 1979 or before. For homes built after 1979, we used literature-
276 reported parameters.⁶ This cutoff of 1979 was based on 10 years after 1969, which is the upper
277 range of the cluster of homes used for parameter estimation.

278 The literature-reported parameters ($\beta_0, \beta_1, \beta_2$) were previously estimated for low-income
279 homes and conventional homes.^{6,26} Low-income homes are residences with household incomes
280 below 125% of the poverty guideline. In this study, household incomes were collected for all
281 homes.

282 We performed a leave-one-out jackknife method to estimate parameters ($\beta_0, \beta_1, \beta_2$) and
283 cross validation for model evaluation.²⁷⁻²⁹ Since the subset of homes with AER measurements
284 had daily window opening data, the LBLX model was used for parameter estimation, and both
285 the LBLX and LBL models were evaluated. We estimated parameters with a subsample of data
286 (training sample) and evaluated the models with the remaining data (validation sample). We
287 removed all samples from one home at a time (validation sample) and estimated parameters with
288 the remaining subsample of data (training sample). We then evaluated the models with the
289 validation sample. This process was performed independently for the low-income homes (n=17)
290 and conventional homes (n=6) to yield two sets of parameters. Each of the 23 homes was used as
291 a validation sample to yield 17 and 6 parameter sets for low-income and conventional homes,
292 respectively. The jackknife estimates were then determined for the low-income homes and the
293 conventional homes (Supplementary Material).

294 Each parameter set was estimated using the least-squares method. Let $Y(x, d; \underline{\beta})$ be the
295 LBLX model-predicted AER in the x^{th} home on the d^{th} day with parameter set $\underline{\beta} = (\beta_0, \beta_1, \beta_2)$. Let
296 $Y_{x,d}$ be the measured AER in the x^{th} home on the d^{th} day. Then, the least squares estimate,
297 $\underline{\beta}^* = (\beta_0^*, \beta_1^*, \beta_2^*)$ is the parameter values $\underline{\beta}$ which minimize the cost function

298 $J(\underline{\beta}) = \sum_{x=1}^N \sum_{d=1}^M [Y(x, d; \underline{\beta}) - Y_{x,d}]^2$ (12)

299 where N is the number homes, and M is the number of days with AER measurements in the x^{th}
300 home.

301 Parameters were estimated with an iterative optimization algorithm. We chose the
302 Nelder-Mead simplex method for its relative insensitivity to the initial parameters values
303 compared with other common methods, such as Newton's method, and its robustness to
304 discontinuities.³⁰ Initial parameter values were set to literature-reported parameters.⁶
305 Convergence to the solution was confirmed after the parameter search terminated.

306

307 ***Model Evaluation Metrics***

308 For model evaluation, we evaluated the differences between individual model-predicted AER
309 ($Y(x, d; \underline{\beta}^*)$) and measured AER ($Y_{x,d}$) using two metrics: relative difference ε (%) and absolute
310 difference Δ (1/h). These metrics are calculated as

311 $\varepsilon = 100 \left(\frac{Y(x, d; \underline{\beta}^*) - Y_{x,d}}{Y_{x,d}} \right)$ (13)

312 $\Delta = Y(x, d; \underline{\beta}^*) - Y_{x,d}$ (14)

313 The absolute difference Δ provides the amount of deviation, and the relative difference ε
314 indicates whether Δ is small or large relative to the measured AER. However, for measured AER
315 with low values, a minor deviation could yield a large ε . In this case, Δ is more meaningful than
316 ε for model evaluation. Therefore, both ε and Δ are used in this study. A positive value for ε and
317 Δ indicates that the model overestimated the measured AER, while a negative value indicates
318 underestimation. Since ε and Δ indicate the bias (i.e., overestimation or underestimation), we
319 also calculated the absolute values $|\varepsilon|$ and $|\Delta|$ to quantify the magnitude of deviation.

320 To compare the modeled and measured AER, we also calculated Pearson and Spearman
321 correlation coefficients. To account for the repeated AER measurements at the homes, we
322 calculated weighted correlation coefficients.³¹ First, each measurement for a given home is
323 replaced with the average measurement for that home. Then, the correlation coefficients were
324 calculated from with the revised values. To determine the amount of variation explained by the
325 AER models, we calculated the coefficient of determination (R^2) as defined by the square of the
326 Pearson correlation coefficient.

327

328 RESULTS

329 For the subset of 24 homes with AER measurements, summary statistics are provided for
330 the number of homes, number of days windows opened, daily measured AER in the two seasons
331 and three road type classifications (Table 1), and building characteristics (Supplementary
332 Material Table S4). Across the 24 homes in the fall and spring, the measured AER varied
333 between 0.09 h^{-1} (minimum) to 3.48 h^{-1} (maximum) with a median of 0.64 h^{-1} . Between the fall
334 and spring, there was no substantial difference in the median AER (0.63 h^{-1} in fall, 0.67 h^{-1} in
335 spring). For the road types, the median AER were highest for HTHD (0.79 h^{-1}) and lowest for
336 HTLD (0.49 h^{-1}).

337 The estimated leakage area (A_{leak}) model parameters for older homes are shown in
338 Table 2. The literature-reported parameters β_0 (low-income and conventional), β_1 (low-income)
339 and β_1 (conventional) for newer homes (Table 3) were different (at 95% confidence level) from
340 the corresponding estimated parameters for the older homes (Table 2).

341

342 *Model Evaluation*

343 Overall, the modeled AERs matched the measured AERs. Summary statistics are
344 provided for the distributions of the modeled and measured AER (Table 1, Supplementary
345 Material Table S6-S7). For the LBLX model, the modeled and measured AER had similar
346 overall medians of 0.64, 0.65 h⁻¹, 25th percentiles of 0.45, 0.42 h⁻¹, and 75th
347 percentiles of 0.99, 0.99 h⁻¹, respectively. For the LBL model, the AER had overall median of 0.64 h⁻¹, 25th and 75th
348 percentiles of 0.43 and 0.97 h⁻¹, respectively, which were slightly lower than the LBLX model.

349 A comparison of the individual modeled and measured AERs is shown for each season
350 and road type (Figure 1, Supplementary Material Figure S3). Overall, the weighted Pearson and
351 Spearman correlation coefficients were 0.78 ($R^2=0.61$) and 0.81 for the LBLX model, and 0.77
352 ($R^2=0.59$) and 0.79 for the LBL model, respectively. Scatter plots of the modeled and measured
353 AER for each home are shown (Supplementary Material Figure S5). The LBLX and LBL
354 showed similar results with the same overall median $|\epsilon|$ of 29%, and median $|\Delta|$ of 0.19 h⁻¹
355 (Figure 1, Supplementary Material Figure S2). The overall median $|\epsilon|$ for the AER models were
356 4% above the estimated PFT measurement uncertainty of 25% (Williams 2009).

357 The LBLX and LBL models showed similar $|\epsilon|$ quartiles for each season and road type
358 (Figure 1, Supplementary Material Figure S3). The LBLX model generally overestimated the
359 AER with overall median ϵ of 6% and median Δ of 0.03 h⁻¹ (Supplementary Material Figure S2).
360 The LBL model also tends to overestimate the AER, but with a slightly smaller overall median ϵ
361 of 5%. For the HTHD road type, the LBLX and LBL models underestimated the AER with
362 overall median ϵ of -14% and -17%, respectively. For the two seasons and the HTLD and LTLD
363 road types, the LBLX and LBL model tended to overestimate the AER.

364 We evaluated the models for the older homes and the one newer home (Figure 2,
365 Supplementary Material Figure S4). For the older homes, the LBLX and LBL models showed

366 similar results with overall median $|\epsilon|$ of 29% and 29%, and median ϵ of 6% and 5%,
367 respectively. Since windows were not opened in the newer home, the LBLX and LBL models
368 had identical results with median $|\epsilon|$ of 17% and median ϵ of 6%.

369 A comparison of the individual modeled and measured AERs is shown for different
370 window openings (Figure 2, Supplementary Material Figure S4). The LBLX and LBL models
371 are equivalent for days with windows closed, and therefore show identical results with median $|\epsilon|$
372 of 29% and median ϵ of 6%. For days with windows opened, the LBLX and LBL models showed
373 similar results with identical overall median $|\epsilon|$ of 26%, and median $|\Delta|$ of 0.24 h^{-1} . However, the
374 LBLX model tends to bias the AER less than the LBL model with ϵ medians of 1% and -14%,
375 respectively.

376

377 *Model Predictions for NEXUS*

378 For applying the LBL model for the health study, we predicted the daily AER (24 h
379 average) for all 213 homes across three years. Summary statistics are provided for the building
380 characteristics (Supplementary Material Table S5). The variability of the daily indoor-outdoor
381 temperature difference, outdoor temperature and wind speed is shown across three years (Figure
382 3B-3D). The modeled AER varied between 0.11 h^{-1} (minimum) and 3.04 h^{-1} (maximum) with
383 25th, 50th, and 75th percentiles of 0.66, 0.95, and 1.28 h^{-1} , respectively (Figure 4). The modeled
384 AER time-course is shown for two homes: homes with highest and lowest median AER
385 predictions (Figure 3A). The slow AER oscillations correspond to variations of the indoor-
386 outdoor temperature differences (Figure 3). The brief AER transients (i.e., positive and negative
387 spikes) correspond primarily to the wind speed variations, and secondarily to indoor-outdoor
388 temperature difference variations (Figure 3). The AER variability is shown for each season and

389 road type (Figure 4). The median modeled AER was highest in the winters (1.36, 1.41, 1.31, and
390 1.24 h⁻¹ for the 4 consecutive winters) and lowest in the summers (0.59, 0.60, 0.63 h⁻¹ for the 3
391 consecutive summers). This seasonal variation corresponded to the median indoor-outdoor
392 temperature differences highest in the winters (26.7, 27.8, 23.3, 22.2 °C for the 4 consecutive
393 winters) and lowest in the summers (0.8, 0.6, 0.0 °C for the 3 consecutive summers), but did not
394 correspond to the wind speeds, which did not vary between seasons. The median wind speeds in
395 winter (12.9, 14.5, 12.9, 12.9 km h⁻¹ for the 4 consecutive winters) and spring (12.9, 12.9, 12.9
396 km h⁻¹ for the 3 consecutive springs) were similar and often slightly higher than the wind speeds
397 in the summer (11.3, 9.7, 11.3 km h⁻¹ for 3 consecutive summers) and fall (11.3, 12.9, 11.3 km
398 h⁻¹ for the 3 consecutive falls). For the HTHD, HTLD, and LTLD road types, the modeled AER
399 were similar with medians of 0.99, 0.89, and 0.96 h⁻¹, and interquartile ranges of 0.64, 0.60, and
400 0.62 h⁻¹, respectively.

401 The variability of the AER predictions is shown for the individual homes within each
402 road type (Figure 5). Across all road types, the modeled AER varied between 0.11 and 0.50 h⁻¹
403 for the minimums, 0.36 and 1.64 h⁻¹ for the medians, and 0.64 and 3.04 h⁻¹ for the maximums.
404 The temporal AER variability of individual homes decreases with decreasing median AER
405 (Figure 3A, Figure 5). Therefore, homes with tighter building envelopes tend to have smaller
406 AER fluctuations from the temporal variability of stack and wind effects.

407

408 DISCUSSION

409 Our goal was to develop daily AER predictions for each NEXUS participant home to provide
410 improved exposure estimates for the health study. We used cross-validation to evaluate two
411 models (LBL and LBLX), which predict residential AER from questionnaires and meteorology,

412 with measured AERs from a subset of NEXUS homes. The daily modeled AER closely
413 correspond to the measured AER with the same overall $|\varepsilon|$ median of 29% for both the LBL and
414 LBLX models. These results demonstrate that it is possible to apply these models for individual-
415 level air pollution exposure assessments that require daily predictions of house-specific AER.

416 We found considerable variation in measured AERs (range: 0.09 - 3.48 h⁻¹) and modeled
417 AERs (range: 0.11 - 3.04 h⁻¹). Another study in central North Carolina showed similar variation
418 in measured AERs (range: 0.09 – 3.17 h⁻¹) across 31 homes on seven consecutive days during the
419 same two seasons (spring, fall) as the seasonal intensives in NEXUS.⁶ This suggest that AER
420 differences may be an important source of heterogeneity in the infiltration of outdoor air
421 pollutants into homes and the resulting exposures, even for studies focused on within-city
422 variations and for studies in different geographical locations. Using questionnaire and weather
423 data, the LBLX and LBL models explained a substantial amount of the measured AER variation
424 ($R^2=61\%$ and 59%, respectively).

425 There is substantial temporal variation in the modeled AER that differs for each home
426 based on the building envelope tightness. The home with the largest A_{leak} (i.e., leakiest building
427 envelope) had the highest median AER (1.64 h⁻¹) and largest AER range (0.50 - 3.04 h⁻¹) across
428 time. The home with the smallest A_{leak} (i.e., tightest building envelope) had the lowest median
429 AER (0.36 h⁻¹) and smallest AER range (0.11 – 0.64 h⁻¹) across time.

430 This study demonstrates a novel health study design and modeling method designed to
431 improve residential AER predictions for individual exposure assessments in health studies. This
432 study is the first to use daily AER measurements and window opening data from a subset of
433 homes for parameter estimation (i.e., model calibration) and model evaluation, and then apply
434 the calibrated model to predict the spatial and temporal variations of the AER for each

435 participant's home in a health study. This approach allowed us to identify where the relative
436 error and bias in the predicted AERs may be important when used in the health effect analyses.
437 For example, the model tended to underestimate AERs for the HTHD homes, while
438 overestimating AERs for the HTLD and LTLD homes.

439 We can compare our model performance using two alternative approaches for parameter
440 estimation of A_{leak} . First, we estimated parameters using both the older and newer homes instead
441 of estimating parameters using the older homes and using literature-reported parameters for the
442 newer home, as described in the methods. Using this alternative method, the median $|\epsilon|$ for the
443 newer home increased from 17% to 91% (Supplementary Material Figure S2, Figure 2). Second,
444 we used the literature-reported parameters for both the older and newer homes instead of only for
445 the newer home, as described in the methods. Using this alternative approach, the median $|\epsilon|$ for
446 the older homes increased from 29% to 43%, the 25th percentile increased from 12% to 19%, and
447 the 75th percentile increased from 63% to 131% (Supplementary Material Figure S2, Figure 2).
448 This demonstrates the benefit of including AER measurements from a subset of homes, which
449 represent the housing stock in the study, to reduce the AER model uncertainty.

450 We can compare the AER model evaluation with other studies. LBL model evaluations
451 using whole-building pressurization measurements to determine the leakage area showed mean
452 $|\epsilon|$ of 26-46% ³² and 25% ³³ for detached homes. For our implementation of the AER models,
453 which uses a leakage area model, the LBL and LBLX models had mean $|\epsilon|$ of 43% and 48%,
454 respectively for 31 detached homes across four seasons in central North Carolina.⁶ In this study,
455 the LBL and LBLX models both had a mean $|\epsilon|$ of 45%. Given the limitations of single-zone
456 AER models (e.g., no internal resistance to airflow, no internal temperature or pressure

457 differences) and the AER measurement error of the PFT method (accuracy of 20-25%, precision
458 of 5-15% for occupied homes),^{18,24,25} our LBL and LBLX model evaluations are reasonable.

459 On days with open windows, similar model evaluation results were obtained for the
460 LBLX model, which includes both leakage and natural ventilation, and the LBL model, which
461 includes only leakage. Another study showed similar results for the LBLX and LBL models with
462 AER measurements and window opening data from 31 homes in central North Carolina.⁶ For
463 253 days with open windows across 4 consecutive seasons, the median $|\varepsilon|$ was 41% and 48% for
464 the LBLX and LBL models, respectively. The LBL and LBLX models may perform similarly
465 since windows may be opened more often on comfortable days with small indoor-outdoor
466 temperature differences. Thus, the stack effect may be small on days with windows opened.
467 Also, the stack effect can be reduced after windows are opened from a thermal equilibrium
468 created between indoor and outdoor temperatures. These results suggest that our application of
469 the LBL model, instead of the LBLX model, for the NEXUS health study is reasonable. In
470 certain geographical locations (e.g., coastal regions) with high and persistent winds, comfortable
471 outdoor temperatures across seasons, and frequent window opening; the LBLX model may
472 provide substantially improved estimates as compared to the LBL model.

473 The temporal resolution of the AER is determined by the meteorological data. In this
474 paper, we used hourly outdoor temperature and wind speed measurements to predict hourly
475 AER, and then calculated 24 h averages to compare with the 24 h average AER measurements.
476 To account for the diurnal variation of traffic-related air pollutants, we plan to use the hourly
477 AER predictions combined with hourly residential outdoor concentration predictions to predict
478 every NEXUS participant's hourly residential indoor concentrations based on the dynamic mass
479 balance model (Equation 3).⁴

480 Since the AER is the key parameter for F_{inf} (Equation 2), we can compare our AER
481 models with a previously reported model used to predict F_{inf} of outdoor PM_{2.5} for individual
482 homes in a health study.¹² The reported F_{inf} model is an empirical model that does not include
483 the stack and wind effects, which are the driving forces for leakage and natural ventilation
484 airflows. This infiltration model also does not account for differences in the leakage area
485 between homes. In our study, the LBL and LBLX models include the stack and wind effects, and
486 the building characteristics that modify the stack effect (i.e., building height) and wind effect
487 (i.e., local wind sheltering and building height). Also, these AER models are linked to a building-
488 specific leakage area model (Equation 5).

489 A limitation of this study is that mechanical ventilation could not be included in the AER
490 predictions for the three year health study since it was not collected due to cost and participant
491 burden considerations. We expect bathroom fans, outdoor-vented kitchen range hoods, and
492 clothes dryers, which have low-intermediate airflows and are used intermittently, to have a small
493 AER effect. Central heating and air conditioning (HVAC) systems in homes re-circulate indoor
494 air with no outdoor air intake, but can have air duct leaks in unconditioned spaces (e.g.,
495 basements, attics) when operated.³⁴ However, none of the NEXUS homes had HVAC systems.
496 Window/wall air conditioners also re-circulate indoor air, but can be operated with open outdoor
497 vents. Other types of outdoor-vented fans include window fans and whole-house fans, which
498 move outdoor air into the living space through open windows. Overall, we expect a large AER
499 effect from window fans, whole-house fans, and window/wall air conditioners operated with
500 open outdoor vents. Attic fans, which ventilate the attic space and not the living space with soffit
501 or gable vents, are expected to have a small AER effect.

Another limitation of this study is that the AER were measured in the spring and fall, with no measurements from the summer or winter due to cost. However, the leakage area model parameters, which were estimated from the AER measurements, are independent of the stack and wind effects that can vary seasonally. Therefore, we expect AER measurements from different seasons to have a small effect on the estimate parameters. In addition, a previous study that compared AER measurements with LBL and LBLX model predictions showed similar results in all four seasons.⁶ Therefore, we expect the model performance in this study to be similar across the four seasons.

This study demonstrates the ability of using a novel method of integrating AER measurements and models to predict the large home-to-home (spatial) and temporal variability of residential AERs, which is an important determinant of exposure heterogeneity in air pollution health studies. Using AER measurements from a subset of homes, we calibrated, evaluated, and applied mechanistic AER models that agree closely to daily AER measurements and explain a substantial amount of the AER variation. Using this novel approach, NEXUS will be one of the first epidemiology studies to apply calibrated and home-specific AER models, and to include the spatial and temporal variations of AER for over 200 individual homes across multiple years into an exposure assessment. This capability will help to provide more accurate exposure estimates for epidemiological studies in support of improving risk estimates.

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542

543 **SUPPLEMENTARY MATERIAL**

544 The supplementary material includes details of the jackknife method for parameter estimation
545 and additional tables and figures.

546

547 **CONFLICTS OF INTEREST**

548 The authors declare no conflict of interest.

549

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675 **FIGURE LEGENDS**

- 676 **Figure 1.** Comparison of absolute differences $|\Delta|$ (A) and relative differences $|\varepsilon|$ (B) between
677 individual modeled and measured AER for each model. Results are separated by season, road
678 type, and across all days. Shown are medians with 25th and 75th percentiles.
- 679
- 680 **Figure 2.** Comparison of absolute differences for $|\Delta|$ (A) and $|\varepsilon|$ (B) between individual modeled
681 and measured AER for the LBLX and LBL models. Results are separated by house age and
682 window status. Shown are medians with 25th and 75th percentiles.

683

684 **Figure 3.** AER predictions for 213 homes across 3 years of health study with results for each
685 season and road type. Boxes correspond to median, 25th and 75th percentiles; and whiskers
686 correspond to minimum and maximum values. Winter includes December, January, and
687 February; spring includes March, April, May; summer includes June, July, August; fall includes
688 September, October, and November. AER oscillations correspond to indoor-outdoor temperature
689 differences. AER transients of positive or negative spikes correspond primarily to wind speeds
690 and secondarily to indoor-outdoor temperature differences.

691

692 **Figure 4.** AER predictions for 213 homes across the 3 years of the health study with results for
693 individual homes grouped by the 3 traffic categories for the homes: HTHD (A), HTLD (B), and
694 LTLD(C). Box plots show median, 25th and 75th percentiles, and minimum and maximum values
695 of 24 h average AER.

696

697 **Figure 5.** Time-course of AER predictions (A), absolute indoor-outdoor temperatures (B),
698 outdoor temperatures (C), and wind speeds (D) across the 3 years of health study. Two AER
699 time-course plots correspond to homes with highest and lowest median AER predictions. Plots
700 show daily 24 h average values across 3 years of health study from January 1, 2010 to December
701 31, 2012.

Table 1. Number of homes, number of days windows opened, and summary statistics for measured 24 h average air exchange rates

Season:year ¹ or road type classification of home	Number of homes	Number of days windows opened ²	Air Exchange Rates (h^{-1})											
			Sample size	Mean	SD	Min	p5	p10	p25	p50	p75	p90	p95	Max
Fall:2010	24	19 (16%)	119	0.74	0.56	0.09	0.12	0.17	0.41	0.63	0.97	1.21	1.69	3.48
Spring:2011	17	9 (12%)	78	0.83	0.48	0.25	0.32	0.35	0.45	0.67	1.06	1.66	1.81	2.05
HTHD ³	7	12 (22%)	55	1.00	0.73	0.11	0.14	0.39	0.53	0.79	1.17	2.01	2.70	3.48
HTLD ³	5	2 (5%)	44	0.65	0.41	0.09	0.13	0.16	0.35	0.49	0.96	1.18	1.52	1.82
LTLD ³	12	14 (14%)	98	0.70	0.39	0.09	0.20	0.25	0.43	0.64	0.91	1.23	1.51	1.80
All	24	28 (14%)	197	0.77	0.53	0.09	0.16	0.25	0.42	0.64	0.99	1.43	1.81	3.48

¹ Fall: September, October, and November; spring: March, April, and May² Percentage of days windows opened relative to corresponding sample size are shown in parentheses³ HTHD: high traffic high diesel, HTLD: high traffic low diesel, LTLD: low traffic low diesel

Table 2. Estimated leakage area model parameters for older homes (built in 1979 or before)

House-type	Parameter ¹	Description	Estimate (95% CI)
Low-Income	β_0	Intercept	6.55×10^1 (2.90×10^1 , 1.02×10^2)
	β_1	Year built	-3.40×10^{-2} (-5.29×10^{-2} , -1.51×10^{-2})
	β_2	Floor area	-7.33×10^{-4} (-9.34×10^{-3} , 7.88×10^{-3})
Conventional	β_0	Intercept	5.69×10^1 (1.77×10^1 , 9.62×10^1)
	β_1	Year built	-2.91×10^{-2} (-4.91×10^{-2} , -9.07×10^{-3})
	β_2	Floor area	-5.65×10^{-3} (-1.39×10^{-2} , 2.58×10^{-3})

¹ β_0 and β_1 are dimensionless, β_2 expressed in units of m⁻²

Table 3. Literature-reported leakage area model parameters for newer homes (built after 1979)

House-type	Parameter ¹	Description	Value
Low-Income	β_0	Intercept	11.1
	β_1	Year built	-5.37×10^{-3}
	β_2	Floor area	-4.18×10^{-3}
Conventional	β_0	Intercept	20.7
	β_1	Year built	-1.07×10^{-2}
	β_2	Floor area	-2.20×10^{-3}

¹ β_0 and β_1 are dimensionless, β_2 expressed in units of m⁻²

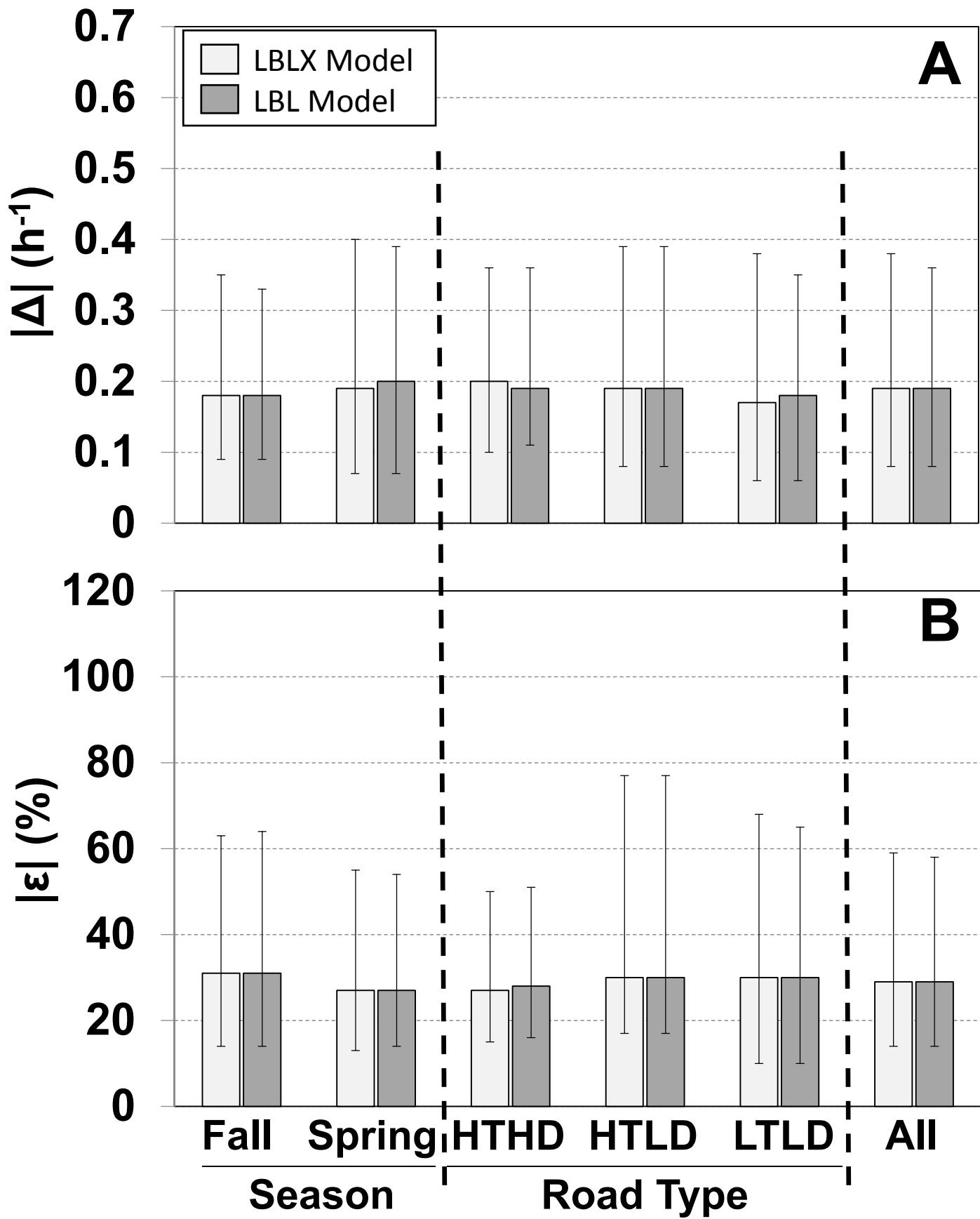


Figure 1

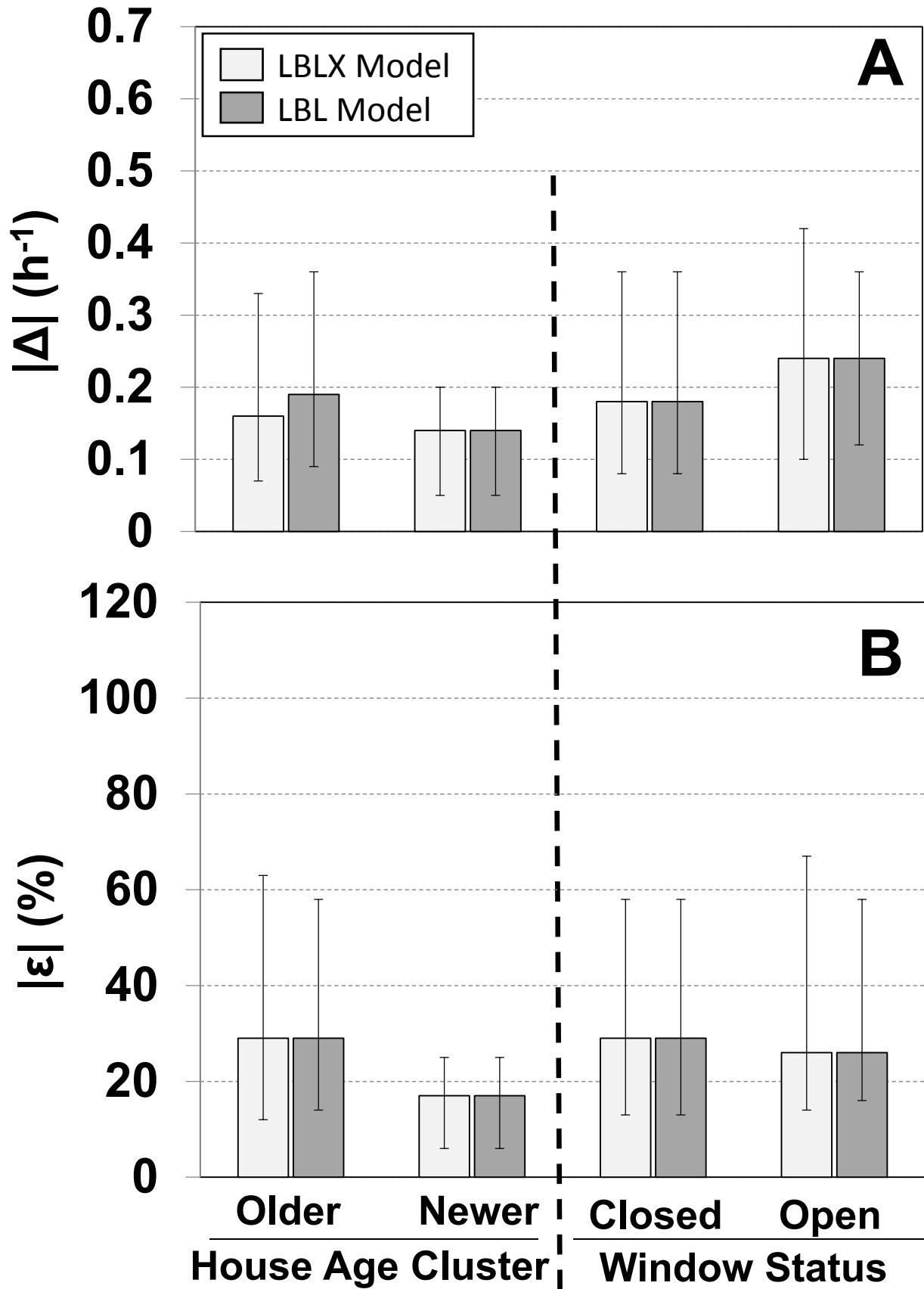


Figure 2

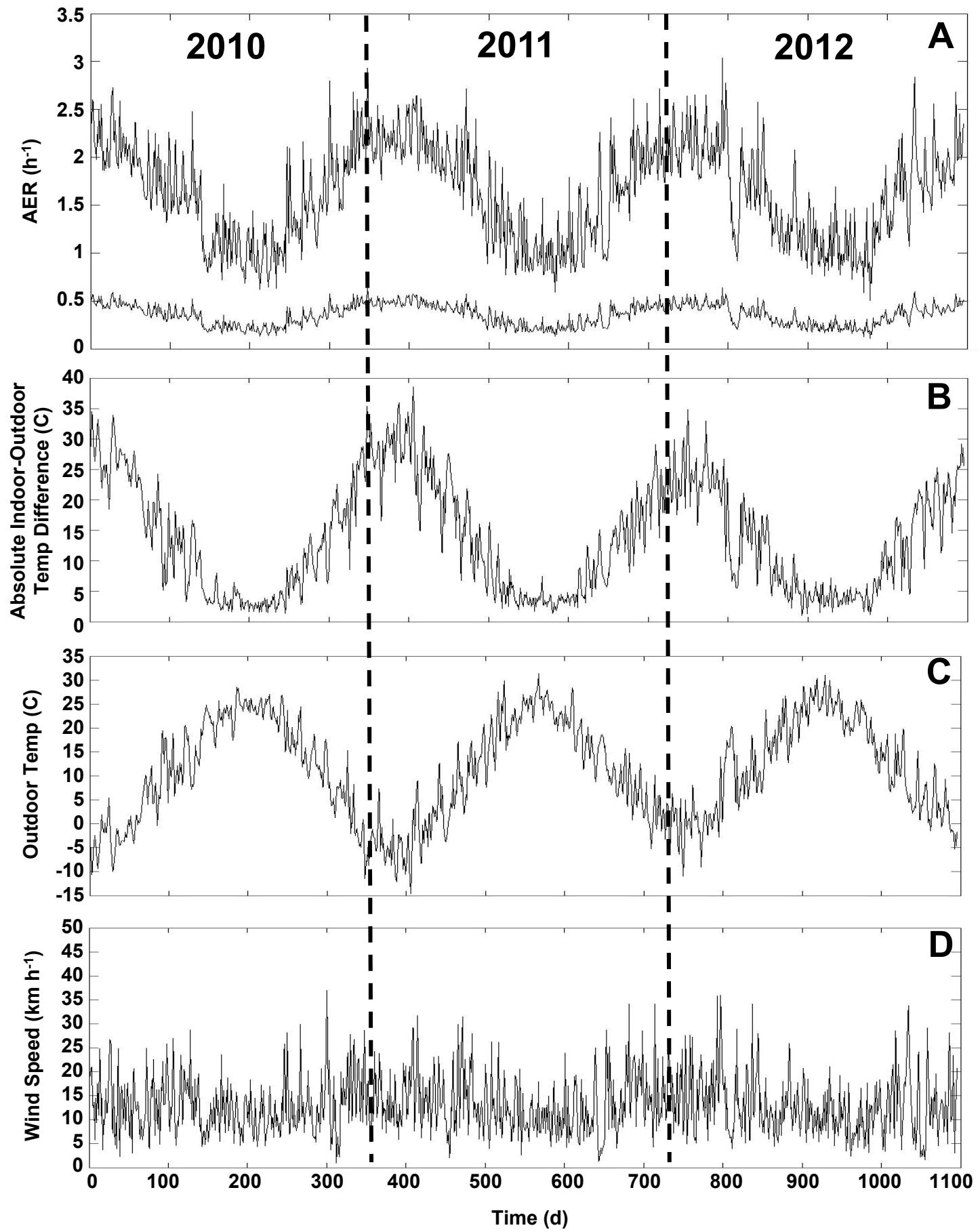


Figure 3

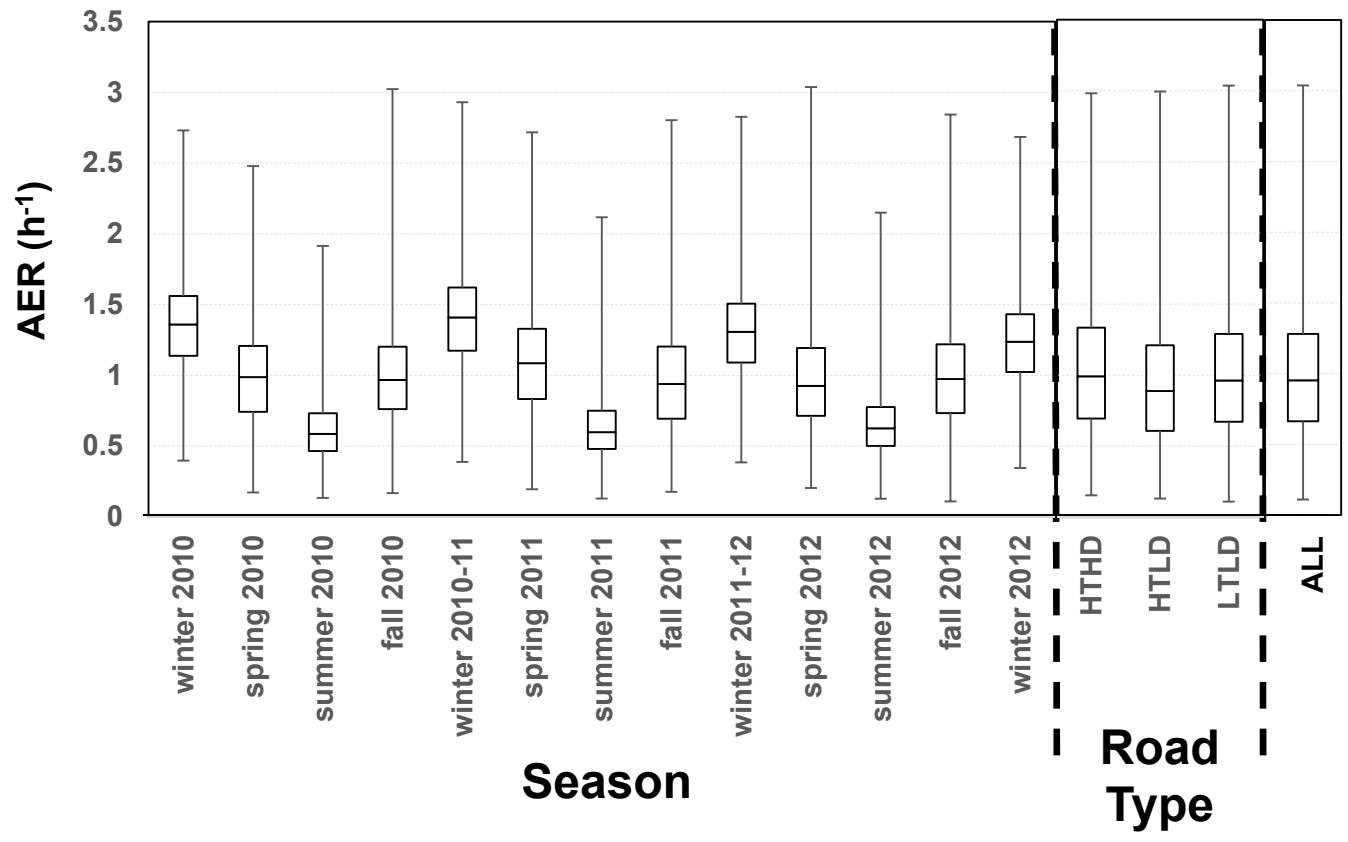


Figure 4

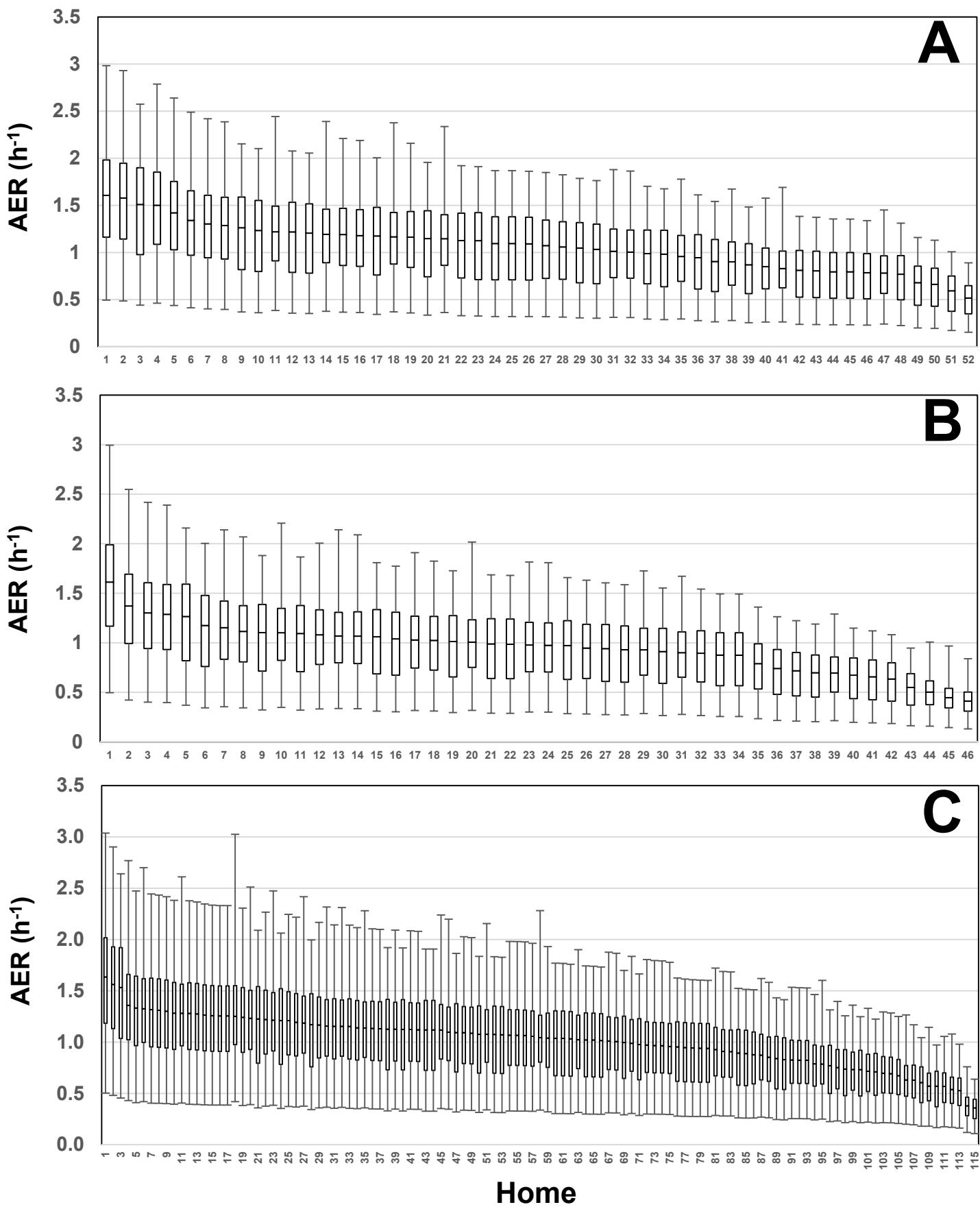


Figure 5