

A bench-scale study on biodegradation and volatilization of ethylbenzoate in aquifers

George X. Yang^{*}, L.E. Erickson, L.T. Fan

Department of Chemical Engineering, Durland Hall, Kansas State University, Manhattan KS 66506-5102, USA

Received 28 July 1995; accepted 28 November 1995

Abstract

Experiments were conducted to investigate the fate of ethylbenzoate and soil microorganisms in shallow aquifers. Biodegradation and volatilization have been identified as the major mechanisms in attenuating ethylbenzoate in contaminated soils. The rate of volatilization was experimentally found to be limited by gas-phase diffusion. The parameters of an available model, i.e., the maximum specific growth rate and the saturation constant, have been estimated by fitting the model to the experimental data obtained with ethylbenzoate as the carbon source; the former was 0.49 h^{-1} , and the latter was 62 mg L^{-1} . Various facets of biodegradation, including the effects of mass-transfer resistance and initial distribution of microorganisms, have been numerically analyzed on the basis of the model.

Keywords: Bioremediation; Aquifer; Volatilization; Mass transfer

1. Introduction

Many aromatic organic chemicals, substituted or unsubstituted, have been on the EPA (Environmental Protection Agency) list of priority pollutants. Once released into the environment, these chemicals pose acute or chronic threats to the health of humans as well as animals. Long-term exposure to benzene causes hemopoietic tissue changes in the form of anemia or leukopenia [1]. Numerous aromatics have been reported to be teratogenic, mutagenic or carcinogenic [1]. Among the technologies for remediating soils contaminated by aromatic chemicals, several involve the principles of biodegradation and volatilization, or the interplay of these two. To quantitatively evaluate the magnitude

^{*} Corresponding author. Tel: (1-913) 532-5584; fax: (1-913) 532-7372.

of biodegradation and volatilization is, therefore, essential for the design and implementation of technologies such as bioventing, air-sparging, plant-based bioremediation, and bio-wall [2–5].

Ethylbenzoate, $C_9H_{10}O_2$, is chosen as a representative contaminant in this study because of its semi-volatile and water-immiscible characteristics. It primarily serves as an organic solvent and is slightly toxic [6]. The LD_{50} oral dose is 2.1 g kg^{-1} for rats and 2.63 g kg^{-1} for rabbits [7]. Ethylbenzoate has a density of 1.05 g cm^{-3} , a water-solubility of 820 mg L^{-1} at 25°C , and a vapor pressure of 1 mm Hg at 44°C . Its Henry's law constant, estimated from the ratio of the vapor pressure to the aqueous solubility, is approximately $0.066 \text{ liter atm/g mole}$ and the dimensionless mole fraction, y/x , is about 3.6 [8]. These values are similar to those of anthracene and ethylene oxide [8,9]; therefore, ethylbenzoate can be regarded as a semi-volatile compound. A dense non-aqueous phase liquid (DNAPL) is formed when ethylbenzoate is present in excess of its water-solubility. One of the objectives of this work is to experimentally assess the relative significance of biodegradation and volatilization in attenuating ethylbenzoate in aquifers. Other objectives are to estimate the parameters in an available model based on the experimental study, to simulate the processes of transport and biotransformation in aquifers, and to numerically analyze the factors affecting the fate of ethylbenzoate.

2. Experimental methods

Experiments entail sample preparation, calibration, and measurement of ethylbenzoate concentrations in the liquid phase, and biodegradation of ethylbenzoate in bench-scale, shallow-bed reactors. These are delineated below.

2.1. Materials

Ethylbenzoate with a grade of 99% (Aldrich Chemical) served as the sole substrate in the experiments; it was used as received. A salt solution prepared for supplying nutrients and pH buffering contained 1000 mg of K_2HPO_4 , 200 mg of KH_2PO_4 , 300 mg of $(NH_4)_2SO_4$, and 100 mg of $MgSO_4 \cdot 7H_2O$ per liter of distilled water; the pH of the solution was measured to be 7.1. Rhizospheric surface soil near Durland Hall, Kansas State University, Manhattan, was collected to obtain a source of microorganisms. The soil, from which visible plant roots and tissues of the soil were removed by forceps, was stored in a refrigerator. Plate Count Agar (Difco Laboratories, Detroit, MI) served as the culturing medium for counting the bacterial population.

2.2. Apparatus and equipment

The experimental setup is illustrated in Fig. 1. Each reactor was a 2 l flask with a rubber stopper through which 1 or more glass tubes, each with a length of 10 cm and an I.D. of 3 mm , were inserted. All reactors were placed in an incubator (New Brunswick Scientific, New Brunswick, NJ) which was maintained at 30°C . The aqueous concentration of ethylbenzoate was measured with a spectrophotometer (Hewlett Packard 8452A).

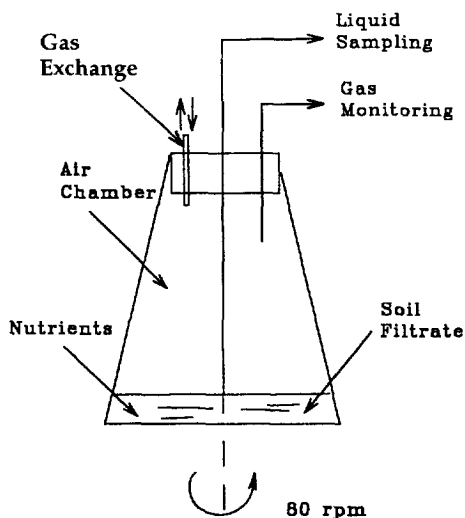


Fig. 1. Experimental set-up: a 2 l-flask fitted with a rubber stopper with a 3 mm glass tube.

Gas composition in the reactors was monitored by a mass-spectrometer (Dycor, Ametek, PA).

2.3. Procedure

For calibrating the spectrophotometer, standard aqueous solutions of ethylbenzoate were prepared. Each sample was extracted twice with equal amounts of cyclohexane; 2 peaks, at 274 nm and 280 nm, were identified to be the absorbance of ethylbenzoate in the UV spectrum [10]. The absorbance was plotted against the aqueous concentration of ethylbenzoate as shown in earlier work [11,12]; the limit of detection of the instrument was 10 mg L^{-1} . The bacteria in the original soil cultured on Plate Count Agar yielded 8.8×10^7 cells per gram of wet soil by plate counting [13]. A drop of Tween 80 (Difco) was added to disperse the microorganisms in the measurement. The moisture content of the soil was determined to be 9.24% by the conventional oven-drying method. A 200 g sample of the soil was mixed with 1 l of the salt solution, blended for 1 min in a household blender, and then centrifuged for 3 min at 9000 rpm. The centrifuged solution was passed through a Whatman No.1 filter paper to further remove particulate solid matter. About 900 ml of final liquid were collected per liter of the salt solution. This liquid had a pH of 8.0 and contained 4.9×10^6 cells ml^{-1} . To 1 liter of the liquid, 0.82 ml of ethylbenzoate was added with a 1 ml syringe, and the mixture was shaken thoroughly for at least 3 min until no ethylbenzoate blobs were visible.

Each of the reactors was filled with 250 ml of aqueous solution to form a 1.5 cm-high shallow pool. These reactors were shaken at 80 rpm in the incubator maintained at 30°C . Liquid and gas samples were withdrawn through hypodermic needles. The reactors were divided into 3 sets. The first set, containing a solution of soil filtrate without ethylbenzoate, was to determine the rate of cell decay. The second set was to

quantify the rate of volatilization; it contained a solution with ethylbenzoate and was sterilized in an autoclave for 30 min at 250 °F and 15 psig. The third set, containing aqueous solution of nutrients and ethylbenzoate, was to measure the rate of biodegradation. Each stopper on the first and third sets of reactors had only 1 glass tube while some stoppers on the second set of reactors had 1 tube, and others had 2. The glass tubes provided openings connecting the gas phase above the simulated aquifer solution with air in the atmosphere; they represent tortuous channels in soils above the aquifer where gas phase diffusion is present.

3. Modelling

Several distinct processes are involved in the attenuation of contaminants in subsurface environments; these processes include volatilization, dissolution, convection, dispersion, adsorption, and chemical and biological degradation. The present study, resorting to batch experiments in well-mixed reactors, focuses on the processes of volatilization, dissolution, and biological degradation.

3.1. Derivation of governing equations

It is assumed that equilibrium is established almost instantaneously between the concentration of ethylbenzoate in the air chamber of a reactor and that in the aqueous solution. This assumption is attributable to the large liquid-air interfacial area and continuous mixing by incubator shaking. The rate of volatilization loss of ethylbenzoate to air, determined by the mass flux through the tubes, is considered to obey a first-order expression; it has the following form [14].

$$j_{AO} = k_m C_s \quad (1)$$

Various models are available to describe the growth of microorganisms through assimilation of substrates. The suitability of each model depends on a variety of factors such as substrate inhibition, substrate competition, microbial acclimation, and oxygen or electron acceptor limitation [15]. The present study adopts the well-known Monod model without neglecting the decay of cells, which accounts for the loss of viable cells. It is assumed that the rate of cell decay is of the first order; furthermore, the rate constant of decay, k_d , is averaged over the whole community of microorganisms.

A mass balance on a reactor gives the governing equation for the substrate, i.e., the contaminant, which is ethylbenzoate in this work,

$$-\frac{dC_s}{dt} = \frac{\mu_m C_b}{Y_s} \left(\frac{C_s}{K_s + C_s} \right) + k_m C_s \frac{A}{V} \quad (2)$$

and also that for biomass,

$$\frac{dC_b}{dt} = \mu_m C_b \left(\frac{C_s}{K_s + C_s} \right) - k_d C_b \quad (3)$$

Complete degradation of an organic chemical usually requires the interplay among various species of microorganisms. It is common for a soil to harbor complex indigenous microbial communities; nonetheless, not all microorganisms in the soil participate in the biodegradation. In this study, therefore, the microorganisms in the soil are divided into 2 categories. One includes those involved in the biodegradation, whose concentration is governed by Eq. (3); the other is those inactive in the biodegradation, whose concentration is governed by the following equation, provided that energy sources are unavailable.

$$\frac{dC_{bi}}{dt} = -k_d C_{bi} \quad (4)$$

Thus, the total biomass concentration, C_{bT} , is

$$C_{bT} = C_b + C_{bi} \quad (5)$$

The effectiveness factor, f_b , is defined in such a way that at $t = 0$,

$$C_b = f_b C_{bT} \quad (6)$$

Since the quantity of a contaminant in the subsurface may exceed the limit of its water solubility, or the rate of mass transfer may be restrained, a distinct non-aqueous phase is frequently present. Under such a circumstance, the rate of dissolution plays an important role in the bioremediation [16]. The non-aqueous phase in soils can exist as discrete or continuous entities with various sizes and shapes, e.g., blobs, channels and films. An organic phase dispersed in water, however, tends to form spheres because of the surface tension. The structures of soils may reshape these spheres by the forces of adhesion, coalescence and emulsification.

By assuming that there are λ non-aqueous organic entities per unit volume of a soil, the mass flux from dissolution of the non-aqueous phase, j_n , is obtained as [16]

$$j_n = \lambda \gamma \sigma \nu k_n (C_{sat} - C_s) \quad (7)$$

To determine j_n according to this equation requires the values of the volume of an entity, ν , the surface-area-to-volume ratio, σ , and the ratio of the aqueous contacting area to the surface area, γ , but it does not require explicit knowledge of the entity's shape. To determine j_n also requires the value of the mass-transfer coefficient, k_n , which can be obtained in many cases from available expressions for estimating it [17].

3.2. Parameter estimation

The parameters to be determined are the mass-transfer coefficient of volatilization, yield factor, maximum specific growth rate, saturation constant, decay constant, and biomass effectiveness factor. In accordance with the experimental design, the following procedure has been established.

When $C_b = 0$, Eq. (2) is integrated to be

$$\ln\left(\frac{C_s}{C_{s0}}\right) = -k'_m t, \quad \left(k'_m = k_m \frac{A}{V}\right) \quad (8)$$

Similarly, Eq. (4) may be integrated to obtain

$$\ln\left(\frac{C_{bi}}{C_{bi0}}\right) = -k_d t \quad (9)$$

The values of k'_m and k_d are obtained by fitting Eq. (8) and Eq. (9), respectively, to the experimental data by minimizing the objective function

$$\sum_{t_i} [\phi(t_i) - \psi(t_i)]^2$$

where $\Phi(t_i)$ is the value of C_s or C_{bi} at time t_i predicted by Eq. (8) or Eq. (9), respectively; and $\Psi(t_i)$ is the corresponding measured value of either variable.

The values of Y_s , μ_m , K_s , and f_b are estimated by minimizing the following objective function by the Adaptive Random Search method (see, e.g., [18]);

$$\sum_k \sum_{t_i} [\phi_k(t_i) - \psi_k(t_i)]^2, (k = s, b)$$

where $\Phi_k(t_i)$ is the value of C_s or C_b at time t_i predicted by simultaneously solving Eq. (2) and Eq. (3) by the second-order modified Euler method [19], and $\Psi_k(t_i)$ is the corresponding experimental data where 's' refers to ethylbenzoate, and 'b' refers to microbial biomass.

4. Results and discussion

In Fig. 2, the measured concentrations of ethylbenzoate are compared with the values predicted by Eq. (8). The area for mass transfer through the stopper of the reactors, each

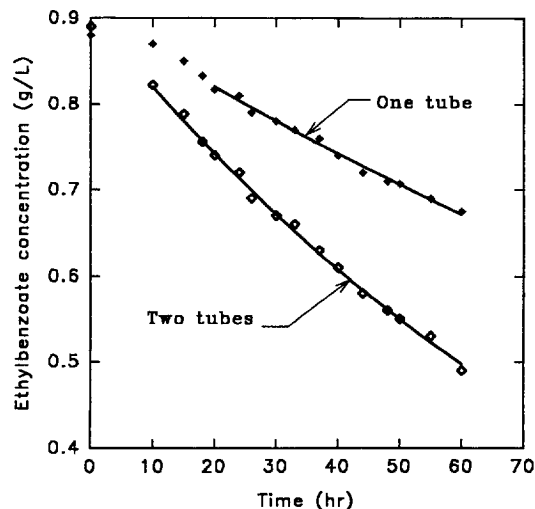


Fig. 2. Model prediction of volatilization of ethylbenzoate compared to the experimental measurements.

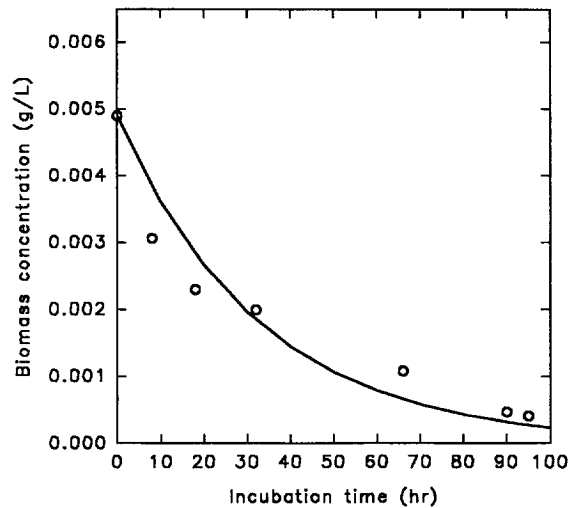


Fig. 3. Comparison of the simulated cell decay with the experimental data.

with 2 tubes, was twice that of the reactors, each with a single tube. The mass-transfer coefficient, k'_m , of the former has been determined to be 0.0102 h^{-1} , which is exactly twice that of the latter, i.e., 0.0051 h^{-1} . Since $k'_m = k_m A/V$, this verifies the assumption of first-order mass transfer. During the experiment, bacteria in the second set of reactors were undetectable, thereby indicating that sterilized environments were achieved throughout the experiment and that the loss of ethylbenzoate was solely due to volatilization. The value of k_d has been estimated to be $3.1 \times 10^{-2} \text{ h}^{-1}$ from the data obtained with the first set of reactors in which microorganisms survived on nutrients without the carbon source (ethylbenzoate); see Fig. 3. The value is relatively large; this may be due to the use of plate counting to follow the viable microbial population. The estimated values of the remaining parameters are reported in Table 1.

Fig. 4 compares the experimentally measured data from the third set of reactors with the values of C_b and C_s predicted by Eq. (2) and Eq. (3) with the parameter values reported in Table 1 under the assumption that a cell had a mass of $1 \times 10^{-12} \text{ g}$ [2,20].

Table 1
Values of the parameters estimated with the experimental data

Parameter	Estimated value
Mass transfer coefficient, k'_m	0.0051 h^{-1}
Maximum specific growth rate, μ_m	0.49 h^{-1}
Saturation constant, K_s	0.062 g L^{-1}
Endogenous decay coefficient, k_d	0.031 h^{-1}
Yield factor, Y_s	$1.56 \text{ g cell per g substrate}$
Effectiveness factor, f_b	0.34

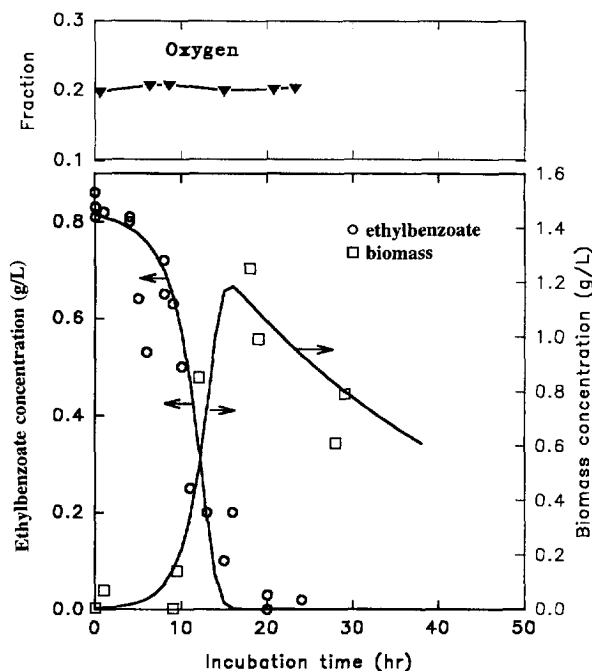
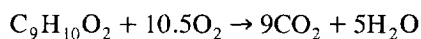


Fig. 4. Comparison between the simulated values and the experimental data for the ethylbenzoate and biomass concentrations.

The relatively large yield of 1.56 g cells/g ethylbenzoate obtained indicates that the average mass of a cell is less than 1×10^{-12} g in this work.

In aerobic environments, the availability of oxygen affects appreciably the rate of biodegradation [21]. The maximum oxygen demand can be calculated from the following stoichiometric formula.



This indicates that 0.205 g of ethylbenzoate in each reactor requires 0.015 mol of O_2 , which is equivalent to 1.11 l of air. The air chamber in a reactor is 1.75 L; furthermore, oxygen transfer is allowed through the tube with a relatively small opening. Thus, the shallow bed reactors are capable of maintaining satisfactory aerobic environments. Fig. 4 shows that the oxygen concentration in the air chamber was stable throughout each experiment.

4.1. Effect of initial biomass concentration

For bioremediation to be effective, participating microorganisms must be genetically robust. The rate of biodegradation depends directly on the concentration of biomass. A sharp increase in microorganism population was observed in each experiment. This phenomenon is demonstrated in Fig. 5 where the process is numerically simulated by Eq. (2) and Eq. (3) with different initial biomass concentrations. Note that microorgan-

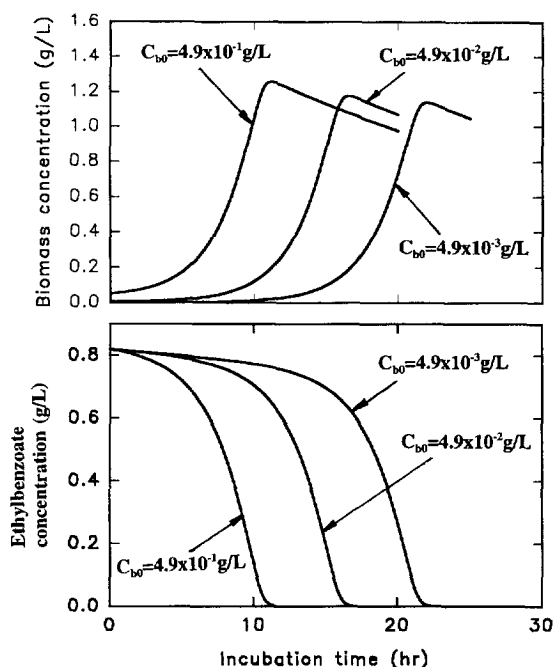


Fig. 5. Model predictions of the ethylbenzoate and biomass concentrations for various initial biomass concentrations.

isms propagate very rapidly as long as the contaminant is available as the food source and nutrients are sufficient.

4.2. Dissolution and biodegradation

The water solubility of an aromatic hydrocarbon is usually low. Suppose that 1% of the liquid volume is occupied by the non-aqueous phase, i.e., pure ethylbenzoate. As such, the total concentration is 11.3 g L^{-1} , of which 7% is in the aqueous solution, while 93% is present as a non-aqueous phase.

It is well known that microorganisms can only survive in environments with low concentrations of some xenobiotic chemicals. An aqueous environment with high concentrations of these chemicals may inhibit or even prevent biotransformation. If the volume fraction of a non-aqueous phase is small, biotransformation of readily biodegradable compounds at the liquid interface or within the non-aqueous phase is insignificant compared to that in the aqueous phase. The rates of microbial assimilation for 2 different biomass concentrations under the condition that biotransformation in the aqueous phase prevails are presented in terms of the aqueous concentration of ethylbenzoate in Fig. 6. This figure also plots the rates of dissolution for 2 different blob sizes simulated under the assumption that the non-aqueous phase comprises discrete spherical

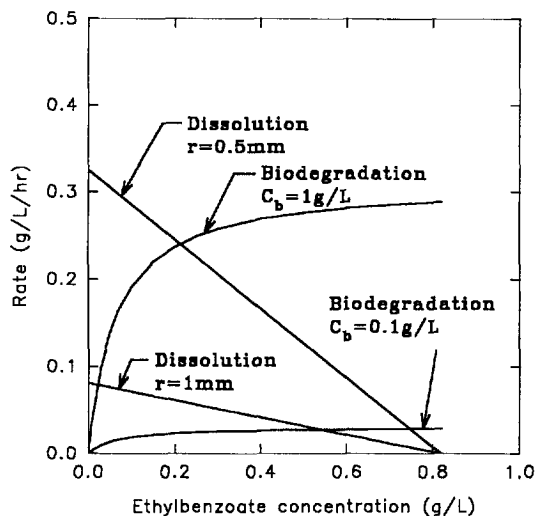


Fig. 6. Comparison of the rates of dissolution and biodegradation for a 1% volume fraction of the non-aqueous phase liquid.

blobs of the same sizes. The dissolution rate is obtained from Eq. (7) in which k_n is calculated by the following 2 equations [14,22].

$$\frac{k_n(2r)}{D_{AB}} = 2 \quad (10)$$

$$D_{AB} = 7.4 \times 10^{-8} \frac{(\psi_B M_B)^{\frac{1}{2}} T}{\mu_B \bar{V}_A^{0.6}} \quad (11)$$

The estimated values of the mass-transfer coefficient, k_n , are $1.83 \times 10^{-4} \text{ cm s}^{-1}$ for $r = 0.5 \text{ mm}$ and $0.915 \times 10^{-4} \text{ cm s}^{-1}$ for $r = 1 \text{ mm}$. It can be discerned from Fig. 6 that when stable biodegradation is established, the rate of biodegradation is always determined by the rate of dissolution. The dissolution rate depends on the mass-transfer coefficient and liquid interfacial area, which, in soils, are determined by factors such as hydrodynamic shear stress and pore structure. Surface tension and adhesive force may cause the non-aqueous phase to emulsify with solid particles and water drops to form large ganglia which can substantially reduce the effective mass-transfer area.

4.3. Volatilization and biodegradation

The rate of volatilization is linearly proportional to the mass-transfer area and vapor pressure of a contaminant. Fig. 7 plots the rates of measured volatilization and biodegradation of ethylbenzoate based on the parameter values reported in this work. Note that for 1 gas exchange tube, volatilization is much slower than biodegradation because the area available for mass exchange between the reactor and the outside

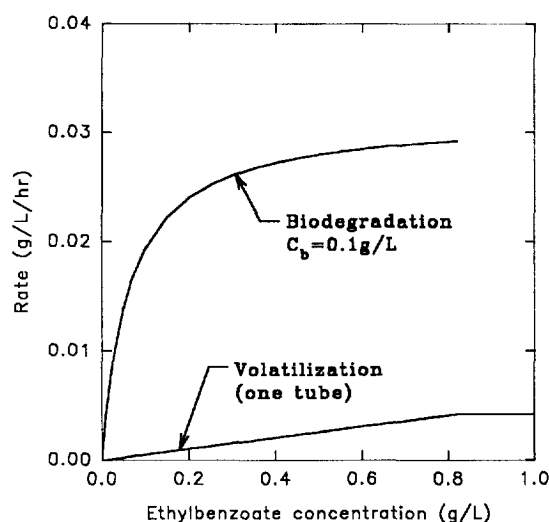


Fig. 7. Comparison of the rates of volatilization and biodegradation.

environment was highly constrained. The experiments mimic a scenario in soils with air channels: the contaminant vapor must disperse through tortuous pore paths to reach these channels. In remediation technologies involving volatilization, transport by diffusion, channelling and bypassing in the soil will dramatically reduce air-contaminant contacting area, thereby lowering their efficiency [23]. Even for semi-volatile compounds, however, volatilization is significant and should not be neglected.

The vapor pressure of an organic chemical is sensitive to temperature. The Antoine equation correlates the vapor pressure with temperature as follows [24]:

$$\log P = A - \frac{B}{C + T} \quad (12)$$

where A , B , and C are constants. The vapor pressure approximately increases exponentially with temperature. Thus, the rate of volatilization is higher at warmer temperatures.

5. Concluding remarks

Experiments were performed in shallow-bed aerobic reactors in which homogeneous environments with a constant concentration of oxygen are maintained for microbial growth. The rates and extent of volatilization and biodegradation were measured in the experiments. The kinetic parameters in a model for simulating attenuation of ethylbenzoate in a mixed culture have been estimated from the resultant experimental data. Parameters obtained include the mass-transfer coefficient of volatilization, maximum specific growth rate, cell decay constant, yield factor, saturation constant, and effectiveness factor of microorganisms involved in biotransformation.

The results of experiments and subsequent numerical simulation indicate that when microorganisms become acclimated to the environment, they propagate very rapidly as long as food sources are sufficient. When a non-aqueous phase exists and the biodegradation in the aqueous phase prevails, the rate of contaminant attenuation is determined by the rate of dissolution of the non-aqueous phase. Finally, volatilization can be significant if air-liquid contacting is allowed to maximally increase the mass-transfer area; furthermore, elevated temperature will enhance the rate of volatilization.

6. Nomenclature

A	area for volatilization, m^2
C_b	biomass concentration involved in the contaminant degradation, M m^{-3}
C_{bi}	biomass concentration not involved in the contaminant degradation, M m^{-3}
C_{bi0}	initial biomass concentration, M m^{-3}
C_{bT}	total biomass concentration, M m^{-3}
C_s	contaminant concentration, M m^{-3}
C_{sat}	contaminant solubility in water, M m^{-3}
C_{s0}	initial contaminant concentration, M m^{-3}
D_{AB}	diffusion coefficient, $\text{m}^2 \text{s}^{-1}$
f_b	effectiveness factor of the biomass concentration
j_{A0}	volatilization flux, $\text{M m}^{-2} \text{s}^{-1}$
j_n	dissolution flux, $\text{M m}^{-3} \text{s}^{-1}$
k_d	decay constant, s^{-1}
k_m	mass transfer coefficient, m s^{-1}
k'_m	mass transfer coefficient ($= k_m A/V$), s^{-1}
k_n	mass transfer coefficient, m s^{-1}
K_s	saturation constant, M m^{-3}
M_B	molecular weight of solvent
P	vapor pressure, $\text{M m}^{-1} \text{s}^{-2}$
r	radius of the non-aqueous phase liquid blob, m
t	time, s
T	temperature, K
v	volume of the non-aqueous phase liquid blob, m^3
V	volume of liquid in a reactor, m^3
\bar{V}_A	specific volume of a solute, $\text{m}^3 \text{M}^{-1}$
Y_s	yield factor
γ	ratio of the aqueous contacting area to the surface area of the non-aqueous phase liquid blob
λ	number distribution of the non-aqueous phase liquid blobs, m^{-3}
μ_B	viscosity, $\text{M m}^{-1} \text{s}^{-1}$
μ_m	maximum specific growth rate of biomass, s^{-1}
σ	surface area-to-volume ratio of the NAPL blob, m^{-1}
Φ	predicted value of a variable
Ψ	measured value of a variable
ψ_B	constant

Acknowledgements

Although the research described in this article has been funded in part by the United States Environmental Protection Agency under assistance agreements R-815709 and R-819653 to the Great Plains-Rocky Mountain Hazardous Substance Research Center for U.S. EPA Regions 7 and 8 with headquarters at Kansas State University, it has not been subjected to the Agency's peer and administrative review, and, therefore, may not necessarily reflect the views of the Agency and no official endorsement should be inferred. This research was partially supported by the Kansas State University Center for Hazardous Substance Research.

References

- [1] WHO (World Health Organization), *Guidelines for Drinking-Water Quality*, Vol. 2, Health Criteria and Other Supporting Information, Macmillan, Geneva, 1984, pp. 182–189 and pp. 229–232.
- [2] P. Gandhi, X. Yang, L.E. Erickson and L.T. Fan, Modelling the Performance of an in situ Aeration Well, *Proceedings of the 24th Annual Biochemical Engineering Symposium*, Sept. 10, 1994, Estes Park, CO, pp. 1–10.
- [3] D.J. Wilson and A.N. Clarke, Soil vapor stripping, in: D.J. Wilson and A.N. Clarke (Eds.), *Hazardous Waste Site Soil Remediation: Theory and Applications of Innovative Technologies*, Marcel Dekker, New York, NY, 1994, pp. 171–242.
- [4] X. Yang, L.T. Fan and L.E. Erickson, Bio-wall Technology: Conceptual Design and Analysis, *AIChE Summer National Meeting*, July 30 – 2 Aug., 1995, Boston, MA, USA.
- [5] M. Narayanan, L.C. Davis and L.E. Erickson, Fate of Volatile Chlorinated Organic Compounds in a Laboratory Chamber with Alfalfa Plants, *Environ. Sci. Technol.*, 29 (1995) 2437–2444.
- [6] W.H. Lederer, *Regulatory Chemicals of Health and Environmental Concern*, Van Nostrand Reinhold, New York, NY, 1995, p. 132.
- [7] R.J. Lewis (Ed.), *Registry of Toxic Effects of Chemical Substances*, National Institute of Occupational Safety and Health, Cincinnati, OH, 1978.
- [8] Y.L. Hwang, J.D. Olsen and G.E. Keller, Steam Stripping for Removal of Organic Pollutants from Water, 2. Vapor-liquid Equilibrium Data, *Ind. Eng. Chem. Res.*, 31 (1992) 1759–1768.
- [9] D. Mackay and W.Y. Shiu, A Critical Review of Henry's Law Constants for Chemicals of Environmental Interest, *J. Phys. Chem. Ref. Data*, 10 (1981) 1175–1199.
- [10] ASTM, *Standard Practice for Identification of Chemicals in Water by Fluorescence Spectroscopy*, Vol 11.02, D4763-88, 1989, pp. 26–31.
- [11] X. Yang, *Characterizing In Situ Bioremediation of Organic Contaminated Soils*, Ph.D. Dissertation, Kansas State University, Manhattan, KS, 1995.
- [12] X. Yang, L.E. Erickson and L.T. Fan, Role of Biodegradation in the Attenuation of Ethylbenzoate in Aquifers, in L.E. Erickson, D.L. Tillison, S.C. Grant and J.P. McDonald (Eds.), *Proceedings of the Tenth Annual Conference on Hazardous Waste Research*, Kansas State University, Manhattan, KS, 1995, pp. 41–50.
- [13] A.G. Wollum II, Cultural Methods for Soil Microorganisms, in: A.L. Page, R.H. Miller and D.R. Keeney (Eds.), *Methods for Soil Analysis*, Agron. Monograph 9, 1982, pp. 781–802.
- [14] R.B. Bird, W.E. Stewart and E.N. Lightfoot, *Transport Phenomena*, John Wiley and Sons, New York, NY, 1960, pp. 3–647.
- [15] J.E. Bailey and D.F. Ollis, *Biochemical Engineering Fundamentals*, 2nd edn., McGraw-Hill, New York, NY, 1986, pp. 86–157.
- [16] X. Yang, L.E. Erickson and L.T. Fan, A Discrete Blob Model of Contaminant Transport in Groundwater with Trapped Non-aqueous Phase Liquids, *Chemical Engineering Communications*, in press (1996).
- [17] E.L. Cussler, *Diffusion*, Cambridge University Press, New York, NY, 1984, pp. 98–99.

- [18] H.T. Chen and L.T. Fan, Multiple Minima in a Fluidized Reactor-Heater System, *AIChE J.*, 22 (1976) 680–685.
- [19] X. Yang, L.E. Erickson and L.T. Fan, A Study of the Dissolution Rate-limited Bioremediation of Soils Contaminated by Residual Hydrocarbons, *J. of Hazardous Materials*, 41 (1995) 299–313.
- [20] Y. Chen, L.M. Abriola, P.J.J. Alvarez, P.J. Anid and T.M. Vogel, Modelling Transport and Biodegradation of Benzene and Toluene in Sandy Aquifer Material: Comparisons with Experimental Measurements, *Water Resour. Res.*, 28 (1992) 1833–1847.
- [21] X. Yang, L.E. Erickson and L.T. Fan, Dispersive-convective Characteristics in the Bioremediation of Contaminated Soil with a Heterogeneous Formation, *J. of Hazardous Materials*, 38 (1994) 163–185.
- [22] C.R. Wilke and P. Chang, Correlation of Diffusion Coefficients in Dilute Solutions, *AIChE Journal*, 1 (1955) 264–270.
- [23] C. Schaefer, R. Arands, H. van der Sloot and D.S. Kosson, Prediction and Experimental Validation of Liquid Phase Diffusion Resistance in Unsaturated Soils, *J. Contaminant Hydrology*, 20 (1995) 145–166.
- [24] B.G. Kyle, *Chemical and Process Thermodynamics*, Prentice Hall, Englewood Cliffs, NJ, 1992, pp. 183–184.